Learning-based Power and Runtime Modeling for Convolutional Neural Networks

Ermao Cai

DAP Committee members:

Aarti Singh (*aartisingh*@*cmu.edu*) (Machine Learning Department) Diana Marculescu (*dianam*@*cmu.edu*) (Department of ECE)

Abstract

With the increased popularity of convolutional neural networks (CNNs) deployed on the widespectrum of platforms (from mobile devices to workstations), the related power, runtime, and energy consumption have drawn significant attention. From lengthening battery life of mobile devices to reducing the energy bill of datacenters, it is important to understand the efficiency of CNNs during serving for making an inference, before actually training the model. In this work, we propose NeuralPower: a layer-wise predictive framework based on sparse polynomial regression, for predicting the serving power, runtime, and energy consumption of a CNN deployed on any GPU platform. Given the architecture of a CNN, NeuralPower provides an accurate prediction and breakdown for power and runtime across all layers in the whole network, helping machine learners quickly identify the power, runtime, or energy bottlenecks. The experimental results show that the prediction accuracy of the proposed *NeuralPower* outperforms the best published model to date, yielding an improvement in accuracy of up to 68.5%. We also assess the accuracy of predictions at the network level, by predicting the runtime, power, and energy of state-of-the-art CNN architectures, achieving an average accuracy of 88.24% in runtime, 88.34% in power, and 97.21% in energy. We comprehensively corroborate the effectiveness of NeuralPower as a powerful framework for machine learners by testing it on different GPU platforms.

1. Introduction

In recent years, convolutional neural networks (CNNs) have been widely applied in several important areas, such as text processing and computer vision, in both academia and industry. However, the high energy consumption of CNNs has limited the types of platforms that CNNs can be deployed on, which can be attributed to both (a) high power consumption and (b) long runtime. GPUs have been adopted for performing CNN-related services in various computation environments ranging from data centers, desktops, to mobile devices. In this context, resource constraints in GPU platforms need to be considered carefully before running CNN-related applications.

In this report, we focus on the *testing* or *service* phase since, CNNs are typically deployed to provide services (*e.g.*, image recognition) that can potentially be invoked billions of times on millions of devices using the same architecture. Therefore, testing runtime and energy are critical to both users and cloud service providers. In contrast, training a CNN is usually done once. Orthogonal to many methods utilizing hardware characteristics to reduce energy consumptions, CNN architecture optimization in the design phase is significant. In fact, given the same performance level (*e.g.*, the prediction accuracy in image recognition task), there are usually many CNNs with different energy consumptions. Figure 1 shows the relationship between model testing errors and energy consumption for a variety of CNN architectures. We observe that several architectures can achieve a similar accuracy level. However, the energy consumption drastically differs among these architectures, with the difference as large as $40 \times$ in several cases. Therefore, seeking for energy-efficient CNN architectures



tecture without compromising performance seems intriguing, especially for large-scale deployment.

DAP

Figure 1: Testing error vs. energy consumption for various CNN architectures on CIFAR-10 running with TensorFlow on Nvidia Titan X GPU. Each point represents one randomly-sampled CNN architecture for making inferences on CIFAR-10. For the architectures that achieve similar error rates (around 20%) during test phase, the energy consumption can vary significantly by more than 40×.

To identify energy-efficient CNNs, the use of accurate runtime, power, and energy models is of crucial importance. The reason for this is twofold. First, commonly used metrics characterizing CNN complexity (e.g., total $FLOPs^1$) are too crude to predict energy consumption for real platforms. Energy consumption depends not only on the CNN architecture, but also on the software/hardware platform. In addition, it is also hard to predict the corresponding runtime and power. Second, traditional profiling methods have limited effectiveness in identifying energy-efficient CNNs, due to several reasons: 1) These methods tend to be inefficient when the search space is large (e.g., more than 50 architectures); 2) They fail to quantitatively capture how changes in the CNN architectures affect runtime, power, and energy. Such results are critical in many automatic neural architecture search algorithms Zoph and Le (2016); 3) Typical CNNs are inconvenient or infeasible to profile if the service platform is different than the training platform. Therefore, it is imperative to train models for power, runtime, energy consumption of CNNs. Such models would significantly help Machine Learning practitioners and developers to design accurate, fast, and energy-efficient CNNs, especially in the design space of mobile or embedded platforms, where power- and energy-related issues are further exacerbated.

In this report, we develop a predictive framework for power, runtime, and energy of CNNs during the testing phase, namely *NeuralPower*, *without* actually running (or implementing) these CNNs on a target platform. The framework is shown in Figure 2. That is, given (a) a CNN architecture of interest and (b) the target platform where the CNN model will be deployed, *NeuralPower* can directly predict the power, runtime, and energy consumption of the network in service/deployment phase. This report brings the following contributions:

- To the best of our knowledge, our proposed learning-based polynomial regression approach, namely *NeuralPower*, is the first framework for predicting the *power consumption* of CNNs running on GPUs, with an average accuracy of 88.34%.
- *NeuralPower* can also predict *runtime* of CNNs, which outperforms state-of-the-art analytical models, by achieving an improvement in accuracy up to 68.5% compared to the best previously published work.

2

^{1.} FLOP stands for "floating point operation".



- Figure 2: *NeuralPower* quickly predicts the power, runtime, and energy consumption of a CNN architecture during service phase. Therefore, *NeuralPower* provides the machine learners with analysis and guidance when searching for energy-efficient CNN architectures on given software/hardware platforms.
 - *NeuralPower* uses power and runtime predictions to predict the *energy consumption* of CNNs running on GPUs, with an average accuracy of 97.21%.
 - In addition to total runtime and average power, *NeuralPower* also provides the detailed breakdown of runtime and power across different components (at each layer) of the whole network, thereby helping machine learners to identify efficiently the runtime, power, or energy bottlenecks.

1.1. Background and Related Work

Prior art, *e.g.*, by Han et al. (2015), has identified the runtime overhead and power consumption of CNNs execution to be a significant concern when designing accurate, yet power- and energy-efficient CNN models. These design constraints become increasingly challenging to address, especially in the context of two emerging design paradigms, (i) the design of larger, power-consuming CNN architectures, and (ii) the design of energy-aware CNNs for mobile platforms. Hence, a significant body of state-of-the-art approaches aim to tackle such runtime and power overhead, by accelerating the execution of CNNs and/or by reducing their power-energy consumption.

To enable CNN architectures that execute faster, existing work has investigated both hardwareand software-based methodologies. On one hand, with respect to hardware, several hardware platforms have been explored as means to accelerate the CNN execution, including FPGA-based methodologies by Zhang et al. (2015a), ASIC-like designs by Zhang et al. (2015b). On the other hand, with respect to software-based acceleration, several libraries, such as cuDNN and Intel MKL, have been used in various deep learning frameworks to enable fast execution of CNNs. Among the different hardware and software platforms, GPU-based frameworks are widely adopted both in academia and industry, thanks to the good trade-off between platform flexibility and performance that they provide. In this work, we aim to model the runtime and power characteristic of CNNs executing on state-of-the-art GPU platforms. In the meantime, recent work has focused on limiting the energy and power consumption of CNNs. Several approaches investigate the problem in the context of hyper-parameter optimization. For instance, Rouhani et al. (2016a) have proposed an automated customization methodology that adaptively conforms the CNN architectures to the underlying hardware characteristics, while minimally affecting the inference accuracy. In addition, some approaches include techniques that draw ideas from energy-aware computer system design, such as the methodologies by Han et al. (2015) and Courbariaux et al. (2016).

While all the aforementioned approaches motivate hardware-related constraints as limiting factors towards enabling efficient CNN architecture, to the best of our knowledge there is no comprehensive methodology that models the runtime, power, and eventually the energy of CNN architectures. That is, prior work either relies on proxies of memory consumption or runtime expressed as simplistic counts of the network weights (*e.g.*, as done by Rouhani et al. (2016b)), or extrapolates power-energy values from energy-per-operation tables (as assumed by Han et al. (2015)). Consequently, existing modeling assumptions are either overly simplifying or they rely on outdated technology nodes. Our work successfully addresses these limitations, by proposing power, energy, and runtime models that are validated against state-of-the-art GPUs and Deep Learning software tools.

A work that shares similar insight with our methodology is the *Paleo* framework proposed by Qi et al. (2016). In their approach, the authors present an analytical method to determine the runtime of CNNs executing on various platforms. However, their model cannot be flexibly used across different platforms with different optimization libraries, without detailed knowledge of them. More importantly, their approach cannot predict power and energy consumption.

2. Data

The aim of this report is to build the predictive models for runtime, power, and enegy consumptions on real platforms running CNNs. Therefore, we collect runtime, power data directly from the GPU platforms. Since the data should be large enough for the learning or modeling process, we pick a set of CNNs to represent various kind of CNN architectures used in both academia and industry. We also collect data from different GPU platforms to test the robustness of our methodology. The details are shown below.

2.1. Experiment Platforms

The main modeling and evaluation steps are performed on the platform described in Table 1. Due to the popularity of TensorFlow in the community, we adopt this software platform throughout this report to implement CNNs. To exclude the impact of voltage/frequency changing on the power and runtime data we collected, we keep the GPU in a fixed state and CUDA libraries ready to use by enabling the persistence mode. We use nvidia-smi to collect the instantaneous power per 1 ms for the entire measuring period. Please note that while this experimental setup constitutes our configuration basis for investigating the proposed modeling methodologies, in Section 4.3 we present results of our approach on other GPU platforms, including Nvidia GTX 1070 and Nvidia Jetson TX1.

Table 1: Target platform				
CPU / Main memory	Intel Core-i7 5820K / 32GB			
GPU	Nvidia GeForce GTX Titan X (12GB DDR5)			
GPU max / idle power	250W / 15W			
Deep learning platform	TensorFlow 1.0 on Ubuntu 14			
Power meter	NVIDIA System Management Interface			

2.2. CNN Architectures Investigated

To comprehensively assess the effectiveness of our modeling methodology, we include a set of several CNN architectures which are widely used in either academia or industry. Our analysis includes state-of-the-art configurations, such as the AlexNet by Krizhevsky (2014), VGG-16 & VGG-19 by Simonyan and Zisserman (2014), R-CNN by Ren et al. (2015), NIN network by Lin et al. (2013), CaffeNet by Jia et al. (2014), GoogleNet by Szegedy et al. (2015), and Overfeat by Sermanet et al. (2013). We also consider different flavors of smaller networks such as vanilla CNNs used on the MNIST by LeCun et al. (1998) and CIFAR10-6conv Courbariaux et al. (2015) on CIFAR-10. This way, we can cover a wide spectrum of CNN applications.

2.3. Data Collection

To train the layer-level predictive models, we collect data points by profiling power and runtime from all layers of all the considered CNN architectures in the training set. We separate the training data points into groups based on their layer types. In this report for the GTX Titan X platform, the training data include 858 convolution layer samples, 216 pooling layer samples, and 116 fully connected layer samples. The statistics can change if one needs any form of customization. For testing, we apply our learned models on the network in the testing set, and compare our predicted results against the actual results profiled on the same platform, including both layer-level evaluation and network-level evaluation.

3. Methodology

In this section, we introduce our hierarchical power and runtime model framework: *NeuralPower*. *NeuralPower* is based on the following key insight: despite the huge amount of different CNN variations that have been used in several applications, all these CNN architectures consist of basic underlying building blocks/primitives which exhibit similar execution characteristics per type of layer. To this end, *NeuralPower* first models the power and runtime of the key layers that are commonly used in a CNN. Then, *NeuralPower* uses these models to predict the performance and runtime of the entire network.

3.1. Layer-Level Power and Runtime Modeling

The first part of *NeuralPower* is layer-level power and runtime models. We construct these models for each type of layer for both runtime and power. More specifically, we select to model three types of layers, namely the *convolutional*, the *fully connected*, and the *pooling* layer, since these layers carry the main computation load during CNN execution.

We propose a learning-based *polynomial regression model* to learn the coefficients for different layers, and we assess the accuracy of our approach against power and runtime measurements on different GPUs. There are three major reasons for this choice. *First*, in terms of model accuracy, polynomial models provide more flexibility and low prediction error when modeling both power and runtime. The *second* reason is the interpretability: runtime and power have clear physical correlation with the layer's configuration parameters (*e.g.*, batch size, kernel size, *etc.*). That is, the features of the model can provide an intuitive encapsulation of how the layer parameters affect the runtime and power. The *third* reason is the available amount of sampling data points. Polynomial models allow for adjustable model complexity by tuning the degree of the polynomial, ranging from linear model to polynomials of high degree, whereas a formulation with larger model capacity may be prone to overfitting. To perform model selection, we apply ten-fold cross-validation and we use Lasso to decrease the total number of polynomial terms. The detailed model selection process will be discussed in Section 4.1.

Layer-level runtime model: The runtime \hat{T} of a layer can be expressed as:

$$\hat{T}(\mathbf{x}_T) = \sum_j c_j \cdot \prod_{i=1}^{D_T} x_i^{q_{ij}} + \sum_s c'_s \mathcal{F}_s(\mathbf{x}_T)$$
(1)
where $\mathbf{x}_T \in \mathbb{R}^{D_T}; \ q_{ij} \in \mathbb{N}; \ \forall j, \ \sum_{i=1}^{D_T} q_{ij} \leq K_T.$

The model consists of two components. The first component corresponds to the regular degree- K_T polynomial terms which are a function of the features in input vector $\mathbf{x}_T \in \mathbb{R}^{D_T}$. x_i is the *i*-th component of \mathbf{x}_T . q_{ij} is the exponent for x_i in the *j*-th polynomial term, and c_j is the coefficient to learn. This feature vector of dimension D_T includes layer configuration hyper-parameters, such as

the batch size, the input size, and the output size. For different types of layers, the dimension D_T is expected to vary. The input vector for every type of layer includes input size. For convolutional layers, the input vector also includes the kernel shape, the stride size, and the padding size. For fully-connected layer, the input vector also includes the output size. For pooling layer, the input vector also includes the size and stride size.

The second component corresponds to special polynomial terms \mathcal{F} , which encapsulate physical operations related to each layer (*e.g.*, the total number of memory accesses and the total number of floating point operations). The number of the special terms differs from one layer type to another. For convolutional layer, the special polynomial terms include the memory access count for input tensor, output tensor, kernel tensor, and the total number of floating point operations for the matrix multiplication. For pooling layer, the special terms include the memory access count for input of floating point operations for the matrix multiplication. For pooling layer, the special terms include the memory access count for input tensors, output tensors and total number of floating point operations for pooling. Finally, c'_s is the coefficient of the *s*-th special term to learn.

Based on this formulation, it is important to note that not all input parameters are positively correlated with the runtime. For example, if the stride size increases, the total runtime will decrease since the total number of convolutional operations will decrease. This observation motivates further the use of a polynomial formulation, since it can capture such trends (unlike a posynomial model, for instance).

Layer-level power model: To predict the power consumption \hat{P} for each layer type during *testing*, we follow a similar polynomial-based approach:

$$\hat{P}(\mathbf{x}_{P}) = \sum_{j} z_{j} \cdot \prod_{i=1}^{D_{P}} x_{i}^{m_{ij}} + \sum_{k} z_{k}^{\prime} \mathcal{F}_{k}(\mathbf{x}_{P})$$

$$\text{where } \mathbf{x}_{P} \in \mathbb{R}^{D_{P}}; \ m_{ij} \in \mathbb{N}; \ \forall j, \ \sum_{i=1}^{D_{P}} m_{ij} \leq K_{P}.$$

$$(2)$$

where the regular polynomial terms have degree K_P and they are a function of the input vector $\mathbf{x}_P \in \mathbb{R}^{D_P}$. m_{ij} is the exponent for x_i of the *j*-th polynomial term, and z_j is the coefficient to learn. In the second sum, z'_k is the coefficient of the *k*-th special term to learn.

Power consumption, however, has a non-trivial correlation with the input parameters. More specifically, as a metric, power consumption has inherent limits, *i.e.*, it can only take a range of possible values constrained through the power budget. That is, when the computing load increases, power does not increase in a linear fashion. To capture this trend, we select an extended feature vector $\mathbf{x}_P \in \mathbb{R}^{D_P}$ for our power model, where we include both the original features used in the runtime model, and the logarithmic form of all these features. As expected, the dimension D_P is twice the size of the input feature dimension D_T . A logarithmic scale in our features vector can successfully reflect such a trend, as supported by our experimental results in Section 4.

3.2. Network-Level Power, Runtime, and Energy Modeling

We discuss the network-level models for *NeuralPower*. For the majority of CNN architectures readily available in a Deep Learning models "zoo" (as the one compiled by Jia et al. (2014)), the whole structure consists of and can be divided into several layers in series. Consequently, using our predictions for power and runtime as building blocks, we extend our predictive models to capture the runtime, the power, and eventually the energy, of the entire architecture at the *network level*.

Network-level runtime model: Given a network with N layers connected in series, the predicted total runtime can be written as the sum of the predicted runtime \hat{T}_n of each layer n:

$$\hat{T}_{total} = \sum_{n=1}^{N} \hat{T}_n \tag{3}$$

Network-level power model: Unlike the summation for total runtime, the average power can be obtained using both per layer runtime and power. More specifically, we can represent the average power \hat{P}_{avg} of a CNN as:

$$\hat{P}_{avg} = \frac{\sum_{n=1}^{N} \hat{P}_n \cdot \hat{T}_n}{\sum_{n=1}^{N} \hat{T}_n}$$
(4)

Network-level energy model: From here, it is easy to derive our model for the total energy consumption \hat{E}_{total} of an entire network configuration:

$$\hat{E}_{total} = \hat{T}_{total} \cdot \hat{P}_{avg} = \sum_{n=1}^{N} \hat{P}_n \cdot \hat{T}_n \tag{5}$$

which is basically the scalar product of the layer-wise power and runtime vectors, or the sum of energy consumption for all layers in the model.

4. Experimental Results

In this section, we assess our proposed *NeuralPower* in terms of power, runtime, and energy prediction accuracy at both layer level and network level. Since the models for runtime and power are slightly different from one to another, we discuss them separately in each case. In addition, we validate our framework on other platforms to show the robustness of *NeuralPower*.

4.1. Layer-Level Model Evaluation

4.1.1. MODEL SELECTION

To begin with model evaluation, we first illustrate how model selection has been employed in NeuralPower. In general, NeuralPower changes the order of the polynomial (e.g., D_T in Equation 1) to expand/shrink the size of feature space. NeuralPower applies Lasso to select the best model for each polynomial model. Finally, NeuralPower selects the final model with the lowest cross-validation Root-Mean-Square-Error (RMSE), which is shown in Figure 3.



Figure 3: Comparison of best-performance model with respect to each polynomial order for the fullyconnected layers. In this example, a polynomial order of two is chosen since it achieves the best Root-Mean-Square-Error (RMSE) for both runtime and power modeling. At the same time, it also has the lowest Root-Mean-Square-Percentage-Error (RMSPE).

4.1.2. RUNTIME MODELS

Applying the model selection process, we achieve a polynomial model for each layer type in a CNN. The evaluation of our models is shown in Table 2, where we report the Root-Mean-Square-Error (RMSE) and the relative Root-Mean-Square-Percentage-Error (RMSPE) of our runtime predictions for each one of the considered layers. Since we used Lasso in our model selection process, we also report the model size (*i.e.*, the number of terms in the polynomial) per layer. More importantly, we compare against the state-of-the-art analytical method proposed by Qi et al. (2016), namely Paleo. To enable a comparison here and for the remainder of section, we executed the Paleo code on the considered CNNs. We can easily observe that our predictions based on the layer-level models clearly outperform the best published model to date, yielding an *improvement in accuracy* up to 68.5% (calculated from the differences of RMSPEs for pooling layer).

Table 2: Comparison of runtime models for common CNN layers – Our proposed runtime model consistently outperforms the state-of-the-art runtime model in both root-mean-square-error (RMSE) and the Root-Mean-Square-Percentage-Error (RMSPE).

Laver type	N	leuralPou	Paleo Qi et al. (2016)		
hay or type	Model size	RMSPE	RMSPE	RMSE (ms)	
Convolutional	60	39.97%	1.019	58.29%	4.304
Fully-connected	17	41.92%	0.7474	73.76%	0.8265
Pooling	31	11.41%	0.0686	79.91%	1.763

Convolutional layer: The convolution layer is among the most time- and power-consuming components of a CNN. To model this layer, we use a polynomial model of degree three. We select a features vector consisting of the batch size, the input tensor size, the kernel size, the stride size, the padding size, and the output tensor size. In terms of the special terms defined in Equation 1, we use terms that represent the total computation operations and memory accesses count.

Fully-connected layer: We employ a regression model with degree of two, and as features of the model we include the batch size, the input tensor size, and the output tensor size. It is worth noting that in terms of software implementation, there are two common ways to implement the fully-connected layer, either based on default matrix multiplication, or based on a convolutional-like implementation (*i.e.*, by keeping the kernel size exactly same as the input image patch size). Upon profiling, we notice that both cases have a tensor-reshaping stage when accepting intermediate results from a previous convolutional layer, so we treat them interchangeably under a single formulation.

Pooling layer: The pooling layer usually follows a convolution layer to reduce the complexity of the model. As basic model features we select the input tensor size, the stride size, the kernel size, and the output tensor size. Using Lasso and cross-validation we find that a polynomial of degree three provides the best accuracy.

4.1.3. Power Models

As mentioned in Section 3.1, we use the logarithmic terms of the original features (*e.g.*, batch size, kernel size, *etc.*) as additional features for the polynomial model since this significantly improves the model accuracy. This modeling choice is well suited for the nature of power consumption which does not scale linearly; more precisely, the rate of the increase in power goes down as the model complexity increases, especially when the power values get closer to the power budget limit. For instance, in our setup, the Titan X GPU platform has a maximum power of 250W. We find that a polynomial order of two achieves the best cross validation error for all three layer types under consideration.

To the best of our knowledge, there is no prior work on power prediction at the layer level to compare against. We therefore compare our methods directly with the actual power values collected from TensorFlow, as shown in Table 3. Once again, we observe that our proposed model formulation achieves error always less that 9% for all three layers. The slight increase in the model size compared to the runtime model is to be expected, given the inclusion of the logarithmic feature terms, alongside special terms that include memory accesses and operations count. We can observe, though, that the model is able to capture the trends of power consumption trained across layer sizes and types.

Table 9. I ower model for common errit layers							
Laver type	NeuralPower						
hay of type	Model size	RMSPE	RMSE (W)				
Convolutional	75	7.35%	10.9172				
Fully-connected	15	9.00%	10.5868				
Pooling	30	6.16%	6.8618				

Table 3: Power model for common CNN layers

4.2. Network-level Modeling Evaluation

With the results from layer-level models, we can model the runtime, power, and energy for the whole network based on the network-level model (Section 3.2) in *NeuralPower*. To enable a comprehensive evaluation, we assess *NeuralPower* on several state-of-the-art CNNs, and we compare against the actual runtime, power, and energy values of each network. For this purpose, and as discussed in Section 2, we leave out a set of networks to be used only for testing, namely the VGG-16, NIN, CIFAR10-6conv, AlexNet, and Overfeat networks.

4.2.1. RUNTIME EVALUATION

Prior to assessing the predictions on the networks as a whole, we show the effectiveness of *Neu*ralPower as a useful aid for CNN architecture benchmarking and per-layer profiling. Enabling such breakdown analysis is significant for machine learning practitioners, since it allows to identify the bottlenecks across components of a CNN.

For runtime, we use state-of-the-art analytical model Paleo as the baseline. In Figure 4, we compare runtime prediction models from *NeuralPower* and the baseline against actual runtime values of each layer in the NIN and VGG-16 networks. From Figure 4, we can clearly see that our model outperforms the Paleo model for most layers in accuracy. For the NIN, our model clearly captures that *conv4* is the dominant (most time-consuming) layer across the whole network. However, Paleo erroneously identifies *conv2* as the dominant layer. For the VGG-16 network, we can clearly see that Paleo predicts the runtime of the first fully-connected layer *fc6* as 3.30 ms, with a percentage prediction error as high as -96.16%. In contrast, our prediction exhibits an error as low as -2.53%. Since layer *fc6* is the dominant layer throughout the network, it is critical to make a correct prediction on this layer.

From the above, we can conclude that our proposed methodology generally has a better accuracy in predicting the runtime for each layer in a complete CNN, especially for the layers with larger runtime values. Therefore, our accurate runtime predictions, when employed for profiling each layer at the network level, can help the machine learners and practitioners quickly identify the real bottlenecks with respect to runtime for a given CNN.

Having demonstrated the effectiveness of our methodology at the layer level, we proceed to assess the accuracy of the network-level runtime prediction \hat{T}_{total} (Equation 3). It is worth observing that in Equation 3 there are two sources of potential error. First, error could result from mispredicting the runtime values \hat{T}_n per layer *n*. However, even if these predictions are correct, another source of



Figure 4: Comparison of runtime prediction for each layer in NIN and VGG-16: Our models provide accurate runtime breakdown of both network, while Paleo cannot. Our model captures the execution-bottleneck layers (*i.e.*, conv4 in NIN, and fc6 in VGG-16) while Paleo mispredicts both.

error could come from the formulation in Equation 3, where we assume that the sum of the runtime values of all the layers in a CNN provides a good estimate of the total runtime. Hence, to achieve a comprehensive evaluation of our modeling choices in terms of both the regression formulation and the summation in Equation 3, we need to address both these concerns.

To this end, we compare our runtime prediction T_{total} against two metrics. *First*, we compare against the actual overall runtime value of a network, notated as T_{total} . *Second*, we consider another metric defined as the sum of the actual runtime values T_n (and not the predictions) of each layer n:

$$\mathbb{T}_{total} = \sum_{n=1}^{N} T_n \tag{6}$$

Intuitively, a prediction value \hat{T}_{total} close to both the \mathbb{T}_{total} value and the actual runtime T_{total} would not only show that our model has good network-level prediction, but that also that our underlying modeling assumptions hold.

We summarize the results across five different networks in Table 4. More specifically, we show the networks' actual total runtime values (T_{total}) , the runtime \mathbb{T}_{total} values, our predictions \hat{T}_{total} , and the predictions from Paleo (the baseline). Based on the Table, we can draw two key observations. First, we can clearly see that our model always outperforms Paleo, with runtime predictions always within 24% from the actual runtime values. Compared to the actual power value, our prediction have an RMSPE of 11.76%, or 88.24% in accuracy. Unlike our model, prior art could underestimate the overall runtime up to 42%. Second, as expected, we see that summing the true runtime values per layer does indeed approximate the total runtime, hence confirming our assumption in Equation 3.

4.2.2. Power evaluation

We present a similar evaluation methodology to assess our model for network-level power predictions. We first use our methodology to enable a per-layer benchmarking of the power consumption. Figure 5 shows the comparison of our power predictions and the actual power values for each layer in the NIN and the VGG-16 networks. We can see that convolutional layers dominate in terms of power consumption, while pooling layers and fully connected layers contribute relatively less. We can also Table 4: Performance model comparison for the whole network. We can easily observe that our model always provides more accurate predictions of the total CNN runtime compared to the best published model to date (Paleo). We assess the effectiveness of our model in five different state-of-the-art CNN architectures.

CNN	Qi et al. (2016)	NeuralPower	Sum of per-layer actual	Actual runtime
name	Paleo (ms)	\hat{T}_{total} (ms)	runtime \mathbb{T}_{total} (ms)	$T_{total} $ (ms)
VGG-16	345.83	373.82	375.20	368.42
AlexNet	33.16	43.41	42.19	39.02
NIN	45.68	62.62	55.83	50.66
Overfeat	114.71	195.21	200.75	197.99
CIFAR10-6conv	28.75	51.13	53.24	50.09

observe that the convolutional layer exhibits the largest variance with respect to power, with power values ranging from 85.80W up to 246.34W.

Another key observation is related to the fully-connected layers of the VGG-16 network. From Figure 4, we know layer fc6 takes the longest time to run. Nonetheless, we can see in Figure 5 that its power consumption is relatively small. Therefore, the energy consumption related of layer fc6 will have a smaller contribution to the total energy consumption of the network relatively to its runtime. It is therefore evident that using only the runtime as a proxy proportional to the energy consumption of CNNs could mislead the machine learners to erroneous assumptions. This observation highlights that power also plays a key role towards representative benchmarking of CNNs, hence illustrating further the significance of accurate power predictions enabled from our approach.



Figure 5: Comparison of power prediction for each layer in NIN and VGG-16.

As discussed in the runtime evaluation as well, we assess both our predictive model accuracy and the underlying assumptions in our formulation. In terms of average power consumption, we need to confirm that the formulation selected in Equation 4 is indeed representative. To this end, besides the comparison against the actual average power of the network P_{avg} , we compare against the average value \mathbb{P}_{avg} , which can be computed by replacing our predictions \hat{P}_n and \hat{T}_n with the

CNN	NeuralPower	Sum of per-layer actual	Actual power
name	\hat{P}_{total} (W)	power \mathbb{P}_{total} (W)	P_{avg} (W)
VGG-16	206.88	195.76	204.80
AlexNet	174.25	169.08	194.62
NIN	179.98	187.99	226.34
Overfeat	172.20	168.40	172.30
CIFAR10-6conv	165.33	167.86	188.34

Table 5: Evaluating our power predictions for state-of-the-art CNN architectures.

actual per-layer runtime and power values:

$$\mathbb{P}_{avg} = \frac{\sum_{n=1}^{N} P_n \cdot T_n}{\sum_{n=1}^{N} T_n} \tag{7}$$

We evaluate our power value predictions for the same five state-of-the-art CNNs in Table 5. Compared to the actual power value, our prediction have an RMSPE of 11.66%, or 88.34% in accuracy. We observe that in two cases, AlexNet and NIN, our prediction has a larger error, *i.e.*, of 10.47% and 20.48% respectively. This is to be expected, since our formulation for \mathbb{P}_{avg} depends on runtime prediction as well, and as observed previously in Table 4, we underestimate the runtime in both cases.

4.2.3. Energy evaluation

Finally, we use Equation 5 to predict the total energy based on our model. To evaluate our modeling assumptions as well, we compute the energy value \mathbb{E}_{total} based on the actual per-layer runtime and power values, defined as:

$$\mathbb{E}_{total} = \sum_{n=1}^{N} P_n \cdot T_n \tag{8}$$

We present the results for the same five CNNs in Table 6. We observe that our approach enables good prediction, with an average RMSPE of 2.79%, or 97.21% in accuracy.

Table 6: Evaluating our energy predictions for state-of-the-art CNN architectures.

$_{\rm CNN}$	NeuralPower	Sum of per-layer actual	Actual energy
name	\hat{E}_{total} (J)	energy \mathbb{E}_{total} (J)	E_{total} (J)
VGG-16	77.312	73.446	75.452
AlexNet	7.565	7.134	7.594
NIN	11.269	10.495	11.465
Overfeat	33.616	33.807	34.113
CIFAR10-6conv	8.938	8.453	9.433

4.3. Models on Other Platforms

Our key goal is to provide a modeling framework that could be flexibly used for different platforms. To comprehensively demonstrate this property of our work, we extend our evaluation to a different GPU platform, including desktop GPU - Nvidia GTX 1070, and mobile GPU - Nvidia Jetson TX1.

4.3.1. Results on NVIDIA GTX 1070

We first apply our framework to another GPU platform, and more specifically to the Nvidia GTX 1070 with 8GB memory. We repeat the runtime and power data collection by executing Tensorflow, and we train power and runtime models on this platform. The layer-wise evaluation results are shown in Table 7. For these results, we used the same polynomial orders as reported previously for the TensorFlow on Titan X experiments. Moreover, we evaluate the overall network prediction for runtime, power, and energy values and we present the predicted values and the prediction error (denoted as Error) in Table 8. Based on these results, we can see that our methodology achieves consistent performance across different desktop GPU platforms.

Laver type		Runtime			Power	
20,01 0,00	Model size	RMSPE	RMSE (ms)	Model size	RMSPE	RMSE (W)
Convolutional	10	57.38~%	3.5261	52	10.23%	9.4097
Fully-connected	18	44.50%	0.4929	23	7.08%	5.5417
Pooling	31	11.23%	0.0581	40	7.37%	5.1666

Table 7: Runtime and power model for all layers using TensorFlow on GTX 1070.

Table 8: Evaluation of *NeuralPower* on CNN architectures using TensorFlow on GTX 1070.

CNN name	Runtime		Power		Energy	
	Value (ms)	Error	Value (W)	Error	Value (J)	Error
AlexNet	44.82	17.40%	121.21	-2.92%	5.44	13.98%
NIN	61.08	7.24%	120.92	-4.13%	7.39	2.81%

4.3.2. Results on NVIDIA Jetson TX1

In addition to the traditional high-performance GPUs, many of the CNNs are running on the mobile platforms to enable various services locally. Therefore, we apply our models on the mobile platform to show that our method are versatile and widely suitable for various platforms.

We present the per-layer accuracy for runtime and power predictions in Table 9. Different than GTX Titan X or 1070, Jetson TX1 has very limited memory resource and power cap. Therefore, it cannot run large CNNs or CNNs with large batch size. For this reason, the CNN architecture set used for Jetson TX1 is a little bit different than the one used in the previous experiments. However, we can still see that *NeuralPower* is robust on mobile GPU platforms. Furthermore, we evaluate our model on the Cifar10-6conv and NIN networks in Table 10. Different with the results shown for GTX 1070, the results for Jetson TX1 show the trend as underestimating the runtime, and overestimating the power consumption. The similar thing is that they still have similar power, runtime, or energy consumption error level.

According to these results, we can conclude that our methodology achieves consistent performance across different GPU platforms, thus enabling a scalable/portable framework from machine learning practitioners to use across different systems.

4.4. Discussion

We first discuss the characteristics of the features in those chosen models. Here are our observations:

• The special polynomial terms \mathcal{F} (mentioned in Section 3.1) are important to both runtime and power models in every type of layer for all the platforms we have studied. On average, 75.0%

Laver type		Runtime			Power	
hay of type	Model size	RMSPE	RMSE (ms)	Model size	RMSPE	RMSE (W)
Convolutional	44	20.00~%	0.437	48	21.69%	0.825
Fully-connected	12	32.64%	0.871	31	7.72%	0.103
Pooling	53	19.34%	0.2307	37	13.81%	0.315

Table 9: Runtime and power model for all layers using TensorFlow on Jetson TX1.

Table 10: Evaluation of *NeuralPower* on CNN architectures using TensorFlow on Jetson TX1.

CNN name	Runtime		Powe	er	Energy	
01010 100110	Value (ms)	Error	Value (W)	Error	Value (J)	Error
Cifar10-6conv	26.69	-13.10%	11.39	18.79%	0.304	3.23%
NIN	75.38	-8.41%	8.23	2.53%	0.620	-6.09%

of features in special terms are chosen for the model, while 35.6% of the regular polynomial features are chosen.

- There is no single feature which is always important to any prediction model across different platforms. However, for any specific prediction task, *e. g.*, runtime prediction for pooling layer, the supports of coefficient vectors for different platforms share a lot of features in common. Averaged through all the models, 79.8% of the features selected by a model for one platform are also chosen by the model for other platforms.
- In general, runtime and power models are likely to choose different features in any type of layer for any platform. The features shared between runtime and power models only compose 34.5% of the total features appeared in the models on average.

It is important to note that the overhead introduced by *NeuralPower* is very limited. More specifically, *NeuralPower* needs to collect datasets to train the models, however, the overhead for training is very small, e.g., around 30 minutes for GTX Titan X. This includes data collection (under 10 minutes) and model training (less than 20 minutes). The process is done once for a new platform. However, the model training process can be further shorten by exploiting transfer learning, which exploits the similarity between different platforms. For example, we find that the best performing models for GTX 1070 have the same polynomial order as the corresponding models for GTX Titan X. Even for Jetson TX1, nearly all best performing models share the same polynomial order as the corresponding models for GTX Titan X, except the runtime model for fully-connected layers. In this case, the model training process, especially the model selection phase, can be greatly simplified. Therefore, the overhead would be negligible. If the training process starts from the scratch, the overhead can still be offset if the CNN architecture search space is large. Even if machine learners only evaluate a few CNN architectures, *NeuralPower* can still provide the detailed breakdown with respect to runtime, power, and energy to identify bottlenecks and possible improvement directions.

5. Conclusion

With the increased popularity of CNN models, the runtime, power, and energy consumption have emerged as key design issues when determining the network architecture or configurations. In this work, we propose *NeuralPower*, the first holistic framework to provide an accurate estimate of power, runtime, and energy consumption. The runtime model of *NeuralPower* outperforms the current state-of-the-art predictive model in terms of accuracy. Furthermore, *NeuralPower* can be used to provide an accurate breakdown of a CNN network, helping machine learners identify the bottlenecks of their designed CNN models. Finally, we assess the accuracy of predictions at the network level, by predicting the runtime, power, and energy of state-of-the-art CNN configurations. *NeuralPower* achieves an average accuracy of 88.24% in runtime, 88.34% in power, and 97.21% in energy. As future work, we aim to extend our current framework to model the runtime, power, and energy of the networks with more sophisticated parallel structures, such as the ResNet network by He et al. (2016).

References

- Matthieu Courbariaux, Yoshua Bengio, and Jean-Pierre David. Binaryconnect: Training deep neural networks with binary weights during propagations. In Advances in Neural Information Processing Systems, pages 3123–3131, 2015.
- Matthieu Courbariaux, Itay Hubara, Daniel Soudry, Ran El-Yaniv, and Yoshua Bengio. Binarized neural networks: Training deep neural networks with weights and activations constrained to+ 1 or-1. arXiv preprint arXiv:1602.02830, 2016.
- Song Han, Jeff Pool, John Tran, and William Dally. Learning both weights and connections for efficient neural network. In Advances in Neural Information Processing Systems, pages 1135–1143, 2015.
- Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun. Deep residual learning for image recognition. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 770–778, 2016.
- Yangqing Jia, Evan Shelhamer, Jeff Donahue, Sergey Karayev, Jonathan Long, Ross Girshick, Sergio Guadarrama, and Trevor Darrell. Caffe: Convolutional architecture for fast feature embedding. arXiv preprint arXiv:1408.5093, 2014.
- Alex Krizhevsky. One weird trick for parallelizing convolutional neural networks. arXiv preprint arXiv:1404.5997, 2014.
- Yann LeCun, Léon Bottou, Yoshua Bengio, and Patrick Haffner. Gradient-based learning applied to document recognition. *Proceedings of the IEEE*, 86(11):2278–2324, 1998.
- Min Lin, Qiang Chen, and Shuicheng Yan. Network in network. arXiv preprint arXiv:1312.4400, 2013.
- Hang Qi, Evan R Sparks, and Ameet Talwalkar. Paleo: A performance model for deep neural networks. 2016.
- Shaoqing Ren, Kaiming He, Ross Girshick, and Jian Sun. Faster r-cnn: Towards real-time object detection with region proposal networks. In *Advances in neural information processing systems*, pages 91–99, 2015.
- Bita Darvish Rouhani, Azalia Mirhoseini, and Farinaz Koushanfar. Delight: Adding energy dimension to deep neural networks. In Proceedings of the 2016 International Symposium on Low Power Electronics and Design, pages 112–117. ACM, 2016a.
- Bita Darvish Rouhani, Azalia Mirhoseini, and Farinaz Koushanfar. Going deeper than deep learning for massive data analytics under physical constraints. In Proceedings of the Eleventh IEEE/ACM/IFIP International Conference on Hardware/Software Codesign and System Synthesis, page 17. ACM, 2016b.
- Pierre Sermanet, David Eigen, Xiang Zhang, Michaël Mathieu, Rob Fergus, and Yann LeCun. Overfeat: Integrated recognition, localization and detection using convolutional networks. arXiv preprint arXiv:1312.6229, 2013.
- Karen Simonyan and Andrew Zisserman. Very deep convolutional networks for large-scale image recognition. arXiv preprint arXiv:1409.1556, 2014.

- Christian Szegedy, Wei Liu, Yangqing Jia, Pierre Sermanet, Scott Reed, Dragomir Anguelov, Dumitru Erhan, Vincent Vanhoucke, and Andrew Rabinovich. Going deeper with convolutions. In Proceedings of the IEEE conference on computer vision and pattern recognition, pages 1–9, 2015.
- Chen Zhang, Peng Li, Guangyu Sun, Yijin Guan, Bingjun Xiao, and Jason Cong. Optimizing fpga-based accelerator design for deep convolutional neural networks. In *Proceedings of the 2015 ACM/SIGDA International Symposium on Field-Programmable Gate Arrays*, FPGA '15, pages 161–170, 2015a. ISBN 978-1-4503-3315-3.
- Qian Zhang, Ting Wang, Ye Tian, Feng Yuan, and Qiang Xu. Approxann: an approximate computing framework for artificial neural network. In 2016 Design, Automation and Test in Europe Conference and Exhibition, pages 701–706. IEEE, 2015b.
- Barret Zoph and Quoc V Le. Neural architecture search with reinforcement learning. arXiv preprint arXiv:1611.01578, 2016.